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# Pilot Optimization and Power Allocation for OFDM-Based Full-Duplex Relay Networks With IQ-Imbalances

JIN WANG<sup>1</sup>, HAI YU<sup>1</sup>, YONGPENG WU<sup>2</sup>, (Senior Member, IEEE),  
FENG SHU<sup>1,3</sup>, (Member, IEEE), JIANGZHOU WANG<sup>4</sup>, (Fellow, IEEE),  
RIQING CHEN<sup>3</sup>, AND JUN LI<sup>1</sup>, (Senior Member, IEEE)

<sup>1</sup>School of Electronic and Optical Engineering, Nanjing University of Science and Technology, Nanjing 210094, China

<sup>2</sup>Shanghai Key Laboratory of Navigation and Location-Based Services, Shanghai Jiao Tong University, Minhang 200240, China

<sup>3</sup>College of Computer and Information Sciences, Fujian Agriculture and Forestry University, Fuzhou 350002, China

<sup>4</sup>School of Engineering and Digital Arts, University of Kent, Canterbury CT2 7NT, U.K.

Corresponding author: Feng Shu (shufeng0101@163.com)

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**ABSTRACT** In orthogonal frequency division multiplexing relay networks with in-phase and quadrature imbalances and full-duplex relay station (RS), how to optimize pilot pattern and power allocation using the criterion of minimizing the sum of mean square errors (Sum-MSE) for the frequency-domain least-squares channel estimator has a heavy impact on self-interference (SI) cancellation. First, the design problem of pilot pattern is casted as a convex optimization. From the Karush–Kuhn–Tucker conditions, the optimal analytical expression is derived when source and RS powers are given or fixed. Second, under the total transmit power sum constraint of source node and RS, an optimal power allocation (OPA) strategy is proposed to further alleviate the effect of Sum-MSE. Simulation results show that the proposed OPA performs better than equal power allocation (EPA) in terms of Sum-MSE, and the Sum-MSE performance gain increases with deviating  $\rho$  from the value of  $\rho^o$  minimizing the Sum-MSE, where  $\rho$  is defined as the average ratio of the residual SI channel gain at RS to the intended channel gain from source to RS. For example, the OPA achieves approximately 5-dB signal-to-noise ratio gain over EPA by shrinking or stretching  $\rho$  with a factor 4. More importantly, the more  $\rho$  decreases or increases, the more the performance gain becomes significant.

**INDEX TERMS** Full-duplex, IQ imbalances, relay, pilot optimization, power allocation.

## I. INTRODUCTION

With the help of full-duplex (FD) operation, cooperative relay networks can double the spectrum efficiency of the conventional relay networks working in time division duplex (TDD)/frequency division duplex (FDD) way [1]–[4]. This is extremely important for the future wireless communications facing spectrum scarcity [5]–[7]. The major challenge for a full-duplex transceiver is the strong self-interference (SI) from its own transmission [8], [9]. In [10], the SI cancellation process is usually divided into two stages: radio-frequency (RF) cancellation and baseband cancellation. The RF cancellation is to significantly reduce the SI power,

and the baseband digital cancellation is to further remove the residual SI partially. For FD relay systems, how to provide a high-performance channel estimation by designing an appropriate channel estimator and optimizing pilot pattern and power allocation is crucial to efficiently lower the effect of residual SI after RF cancellation [11], [12].

Xiong *et al.* [13] proposed a maximum-likelihood (ML) channel estimator to simultaneously estimate both user-to-relay channels and SI channel at relay station (RS) in large-scale multiple input multiple output (MIMO) relay networks. To further achieve a reduction in the computational complexity of ML, the expectation-maximization (EM) iterative

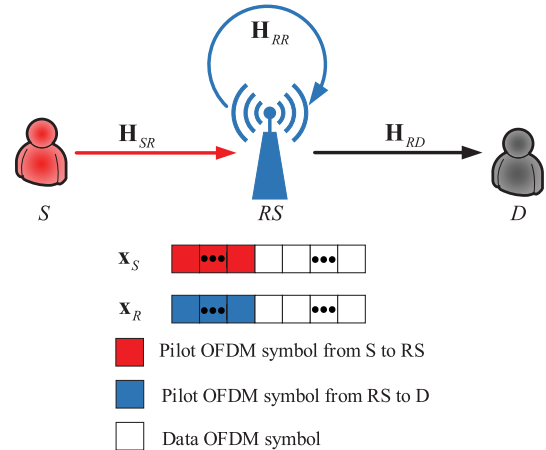
algorithm was adopted to implement the ML. The proposed EM-based ML method showed a better performance than the arithmetic-mean-based one. In [14], the Broyden-Fletcher-Goldfarb-Shanno algorithm was utilized to solve the ML estimator to estimate the intended and residual SI channel at destination in FD two-way relay systems, where pilot pattern was block-type. In practice, the existence of in-phase and quadrature (IQ) imbalance of orthogonal frequency division multiplexing (OFDM) transceivers makes it more complicated to estimate channels due to the destroyed orthogonality between subchannels [15]–[17].

Channel estimation and pilot optimization in FD point-to-point OFDM systems with IQ imbalances were intensively investigated in [18] and [19]. In [18], an adaptive orthogonal matching pursuit based channel estimator was proposed by exploiting the sparsity of both SI and intended channels mixed with IQ parameters. The proposed method performed much better than time-domain least-square (LS) due to exploiting the sparse property of channel. Two LS channel estimators were proposed and their optimal pilot patterns were formalised as a convex optimization problem in [19]. When the transmit power of source was identical with that of destination, the closed-form expression of optimal pilot product matrix was proved to be any four columns of an unitary matrix multiplied by a constant. In this paper, we extend this result to the FD relay networks with IQ imbalance. Here, RS operates in FD mode, and has unequal transmit power as source node. In such a more general scenario, power allocation (PA) becomes a challenging problem. Our main contributions are as follows.

- Fixing both transmit powers of source node and RS, in terms of minimum sum of mean square errors (Sum-MSE), where the two powers are equal or not equal, pilot design is casted as a convex optimization. The optimal pilot pattern is derived for the frequency-domain LS channel estimator using the Karush-Kuhn-Tucker (KKT) conditions. When the transmit powers of source node and RS are identical, the optimal pilot pattern degenerates towards the special form in [19].
- Problem of power allocation is established as a geometric optimization. The optimal power allocation (OPA) strategy is derived and proposed under the total power sum constraint of source node and RS by using the Lagrangian multiplier method. Compared to equal power allocation, the proposed OPA shows a significant improvement in Sum-MSE performance as  $\rho$  deviates far from its optimal feasible value of minimizing the Sum-MSE, where  $\rho$  is defined as the average ratio of channel gain of the residual SI at RS to that from source to RS and a positive number.

The remainder of this paper is organized as follows. Section II describes the full-duplex relay system model with IQ imbalance and the frequency-domain LS channel estimator is applied to for channel estimation. In Section III, the optimal pilot pattern and power allocation are derived to minimize the Sum-MSE. Simulation results are presented in Section IV. Finally, Section V concludes this paper.

*Notations:* Matrices and vectors are denoted by letters of bold upper case and bold lower case, respectively. Signs  $(\cdot)^H$ ,  $(\cdot)^*$ ,  $(\cdot)^T$ ,  $(\cdot)^{-1}$  and  $\text{tr}(\cdot)$  stand for the Hermitian conjugate, conjugate, transpose, inverse, and trace operation, respectively. The notation  $\mathcal{E}\{\cdot\}$  and  $\langle \cdot \rangle_N$  refer to the expectation and modulo operation.  $\mathbf{I}_N$  denotes the  $N \times N$  identity matrix and  $\mathbf{0}_N$  denotes an all-zero matrix of size  $N \times N$ .  $\otimes$  denotes the Kronecker product of two matrices.  $\text{diag}\{\mathbf{a}\}$  represents a diagonal matrix formed by placing all elements of the vector  $\mathbf{a}$  on its main diagonal.



**FIGURE 1. Block diagram of system model with block-type pilot pattern where S, RS, and D are short for source, relay station, and destination, respectively.**

## II. SYSTEM MODEL AND CHANNEL ESTIMATOR

Fig. 1 illustrates an OFDM-based decode-and-forward (DF) relay network consisting of source node (S), destination node (D) and RS. It is assumed that there exists no direct link between source and destination. In this figure, the RS operates in FD mode. It receives the current frame of symbols transmitted from source, and at the same time sends the previous frame of symbols to destination over the same frequency band.  $\mathbf{H}_{SR} \in \mathbb{C}^{N \times 1}$ ,  $\mathbf{H}_{RD} \in \mathbb{C}^{N \times 1}$ , and  $\mathbf{H}_{RR} \in \mathbb{C}^{N \times 1}$  represent the intended source-to-relay, relay-to-destination, and the residual SI frequency-domain channel vectors from RS itself after RF cancellation, respectively, where  $N$  denotes the total number of subcarriers [20]–[22]. Assume all the channels are quasi-static Rayleigh fading, that is, all channel gain vectors keep constant during one frame. Here, one frame may include several hundreds or even thousands of OFDM symbols. For the convenience of derivation and analysis below, block-type pilot pattern is adopted for channel estimation. Each frame includes  $N_P$  successive pilot OFDM symbols and  $N_D$  data OFDM symbols, where  $N_P$  successive pilot OFDM symbols are placed in the beginning of each frame and  $N_D \gg N_P$  such that a high spectrum efficiency is achieved. Here, we assume all transmitters and receivers at source and RS are based on the direction conversion architectures such that the baseband signals are more severely distorted by IQ imbalances compared to the the heterodyne

one [19], [23]. In what follows, by optimizing pilot pattern and power allocation, the effects of IQ-imbalance distortion and SI will be reduced effectively.

Since the imbalances between I and Q components at both the source transmitter and the RS transceiver generate the image of signals and destroy the orthogonality of subcarriers, the received symbol over subcarrier  $k$  of OFDM symbol  $n$  at RS has the form

$$y(n, k) = H_{SR}^{a,n}(k)x_S(n, k) + H_{SR}^{b,n}(k)x_S^*(n, \hat{k}) + \rho H_{RR}^{a,n}(k)x_R(n, k) + \rho H_{RR}^{b,n}(k)x_R^*(n, \hat{k}) + \mu_{r,R}v(n, k) + v_{r,R}v^*(n, \hat{k}) \quad (1)$$

where  $\hat{k} = (N - k + 2)_N$  stands for the index of the image of subcarrier  $k$ .  $x_S(n, k)$  and  $x_R(n, k)$  denote the transmit pilot symbols from source node and RS corresponding to the  $n$ th OFDM symbol over  $k$ th subcarrier with  $E\{|x_S(n, k)|^2\} = P_S$  and  $E\{|x_R(n, k)|^2\} = P_R$ , where  $P_S$  and  $P_R$  are the average signal powers per subcarrier of source node and RS, respectively.

$$H_{SR}^{a,n}(k) = \mu_{r,R}\mu_{t,S}H_{SR}^n(k) + v_{r,R}v_{t,S}^* \left( H_{SR}^n(\hat{k}) \right)^* \quad (2)$$

$$H_{SR}^{b,n}(k) = \mu_{r,R}v_{t,S}H_{SR}^n(k) + v_{r,R}\mu_{t,S}^* \left( H_{SR}^n(\hat{k}) \right)^* \quad (3)$$

$$H_{RR}^{a,n}(k) = \mu_{r,R}\mu_{t,R}H_{RR}^n(k) + v_{r,R}v_{t,R}^* \left( H_{RR}^n(\hat{k}) \right)^* \quad (4)$$

$$H_{RR}^{b,n}(k) = \mu_{r,R}v_{t,R}H_{RR}^n(k) + v_{r,R}\mu_{t,R}^* \left( H_{RR}^n(\hat{k}) \right)^* \quad (5)$$

and

$$\mu_{t,S} = \cos(\theta_{t,S}/2) + j\alpha_{t,S} \sin(\theta_{t,S}/2), \quad (6)$$

$$v_{t,S} = \alpha_{t,S} \cos(\theta_{t,S}/2) - j \sin(\theta_{t,S}/2), \quad (7)$$

where  $\alpha_{t,S}$  and  $\theta_{t,S}$  are amplitude and phase imbalances at transmitter of source node. Similar to (6) and (7), the associated transmit and receive IQ-imbalance parameters at RS are defined as  $\mu_{t,R}$ ,  $v_{t,R}$ ,  $\mu_{r,R}$  and  $v_{r,R}$ , respectively.  $v(n, k)$  is additive Gaussian white noise (AWGN) with zero mean and  $\sigma_v^2$  variance in frequency domain at RS.

It is particularly noted that the scalar parameter  $\rho$  in (1) represents the average ratio of the residual SI channel gain to the intended channel gain, and reflects the relationship of who is dominant between the two channel gains. If  $\rho > 1$ , then the residual SI channel is dominant and stronger than the intended channel. In other words, the useful messages are drowned in the residual SI. If  $\rho < 1$ , then there is a converse result. That is, the intended signal is dominant over the residual SI channel. The value of  $\rho$  depends on the relationship of RF SI cancellation capacity at RS and path loss from source to RS.

The received symbol corresponding to subcarrier  $\hat{k}$  is

$$y(n, \hat{k}) = H_{SR}^{a,n}(\hat{k})x_S(n, \hat{k}) + H_{SR}^{b,n}(\hat{k})x_S^*(n, k) + \rho H_{RR}^{a,n}(\hat{k})x_R(n, \hat{k}) + \rho H_{RR}^{b,n}(\hat{k})x_R^*(n, k) + \mu_{r,R}v(n, \hat{k}) + v_{r,R}v^*(n, k). \quad (8)$$

In order to facilitate the following analysis, let us define  $\mathbf{\Gamma}_{n,k} = [H_{SR}^{a,n}(k) (H_{SR}^{b,n}(\hat{k}))^* H_{SR}^{b,n}(k) (H_{SR}^{a,n}(\hat{k}))^* H_{RR}^{a,n}(k)$

$(H_{RR}^{b,n}(\hat{k}))^* H_{RR}^{b,n}(k) (H_{RR}^{a,n}(\hat{k}))^*]^T$ ,  $\mathbf{x}_{n,k} = [x_S(n, k) x_S^*(n, \hat{k}) x_R(n, k) x_R^*(n, \hat{k})]$ ,  $\mathbf{A} = \text{diag}\{1, 1, 1, 1, \rho, \rho, \rho, \rho\}$ ,  $\mathbf{y}_{n,k} = [y(n, k) y^*(n, \hat{k})]^T$ , and  $\mathbf{w}_{n,k} = [\mu_{r,R}v(n, k) + v_{r,R}v^*(n, \hat{k}) \mu_{r,R}^*v^*(n, \hat{k}) + v_{r,R}v(n, k)]^T$ . Stacking a pair of receive symbols over subcarriers  $k$  and  $\hat{k}$  forms the receive vector

$$\mathbf{y}_{n,k} = (\mathbf{x}_{n,k} \otimes \mathbf{I}_2) \mathbf{A} \mathbf{\Gamma}_{n,k} + \mathbf{w}_{n,k}. \quad (9)$$

In (9), there are eight unknowns but only two measurements. Eq. (9) is under-determined. Hence, at least  $N_P \geq 4$  consecutive OFDM symbols are required to estimate  $\mathbf{\Gamma}_{n,k}$  from (9). Stacking all the receive signals over subcarrier  $k$  and  $\hat{k}$  corresponding to these  $N_P$  OFDM symbols yields

$$\mathbf{y}_k^P = (\mathbf{X}_k^P \otimes \mathbf{I}_2) \mathbf{A} \mathbf{\Gamma}_k + \mathbf{w}_k^P \quad (10)$$

where  $\mathbf{X}_k^P = [\mathbf{x}_{1,k}^T \mathbf{x}_{2,k}^T \cdots \mathbf{x}_{N_P,k}^T]^T$ ,  $\mathbf{y}_k^P = [\mathbf{y}_{1,k}^T \mathbf{y}_{2,k}^T \cdots \mathbf{y}_{N_P,k}^T]^T$ , and  $\mathbf{\Gamma}_k$  is constant from pilot OFDM symbol 1 to  $N_P$ , thus its subscript is omitted for convenience.  $\mathbf{w}_k^P = [\mathbf{w}_{1,k}^T \mathbf{w}_{2,k}^T \cdots \mathbf{w}_{N_P,k}^T]^T$  with the covariance matrix being  $\mathbf{C}_w = E\{\mathbf{w}_k^P (\mathbf{w}_k^P)^H\} = \mathbf{I}_{N_P} \otimes \mathbf{C}_w$  and

$$\mathbf{C}_w = \sigma_v^2 \begin{pmatrix} |\mu_{r,R}|^2 + |v_{r,R}|^2 & 2\mu_{r,R}v_{r,R} \\ 2\mu_{r,R}^*v_{r,R}^* & |\mu_{r,R}|^2 + |v_{r,R}|^2 \end{pmatrix}. \quad (11)$$

Given matrix  $(\mathbf{X}_k^P)^H \mathbf{X}_k^P$  is invertible, the LS channel estimator is expressed as follows

$$\hat{\mathbf{\Gamma}}_k = \mathbf{A}^{-1} \left[ (\mathbf{X}_k^P)^H \mathbf{X}_k^P \right]^{-1} (\mathbf{X}_k^P)^H \otimes \mathbf{I}_2 \mathbf{y}_k^P \quad (12)$$

which gives rise to the channel estimation error

$$\Delta \hat{\mathbf{\Gamma}}_k = \mathbf{\Gamma}_k - \hat{\mathbf{\Gamma}}_k = \mathbf{A}^{-1} \left[ (\mathbf{X}_k^P)^H \mathbf{X}_k^P \right]^{-1} (\mathbf{X}_k^P)^H \otimes \mathbf{I}_2 \mathbf{w}_k^P. \quad (13)$$

From (13), we define the Sum-MSE corresponding to pilot subcarrier pair  $k$

$$\text{Sum-MSE}_k = E\{\text{tr}[\Delta \hat{\mathbf{\Gamma}}_k (\Delta \hat{\mathbf{\Gamma}}_k)^H]\} = \text{tr}\{\mathbf{A}^{-2} [(\mathbf{X}_k^P)^H \mathbf{X}_k^P]^{-1} \otimes \mathbf{C}_w\}. \quad (14)$$

Rewriting  $\mathbf{A} = \mathbf{B} \otimes \mathbf{I}_2$  with  $\mathbf{B} = \text{diag}\{1, 1, \rho, \rho\}$  and using the property of Kronecker product computation [24], the above Sum-MSE is simplified as

$$\text{Sum-MSE}_k = \text{tr}\{\mathbf{B}^{-2} ((\mathbf{X}_k^P)^H \mathbf{X}_k^P)^{-1}\} \text{tr}\{\mathbf{C}_w\}. \quad (15)$$

### III. OPTIMAL PILOT DESIGN AND POWER ALLOCATION

In the previous section, an LS channel estimator and its Sum-MSE expression are presented. In this section, by minimizing its Sum-MSE, we attain its optimal pilot pattern in the convex optimization way. Then, the optimal power allocation policy is casted as a geometric program subject to the total power sum constraint and computed by the KKT conditions.

**A. OPTIMAL PILOT PATTERN**

Firstly, given the transmit powers at source and RS, the design problem of optimal pilot pattern is written as the following optimization

$$\begin{aligned} & \min_{\mathbf{X}_k^p} \text{Sum-MSE}_k \\ & \text{s.t. } \text{tr}\{\mathbf{E}_S^H (\mathbf{X}_k^p)^H \mathbf{X}_k^p \mathbf{E}_S\} \leq 2N_P P_S, \\ & \quad \text{tr}\{\mathbf{E}_R^H (\mathbf{X}_k^p)^H \mathbf{X}_k^p \mathbf{E}_R\} \leq 2N_P P_R \end{aligned} \quad (16)$$

with  $\mathbf{E}_S = [\mathbf{I}_2 \ \mathbf{0}_2]^H$  and  $\mathbf{E}_R = [\mathbf{0}_2 \ \mathbf{I}_2]^H$ . Defining Gram matrix  $\mathbf{Y}_k = (\mathbf{X}_k^p)^H \mathbf{X}_k^p$  and omitting the constant  $\text{tr}\{\mathbf{C}_w\}$ , the above optimization problem will be converted into

$$\min_{\mathbf{Y}_k} \text{tr}\{\mathbf{B}^{-2} \mathbf{Y}_k^{-1}\} \quad (17a)$$

$$\text{s.t. } \text{tr}\{\mathbf{E}_S^H \mathbf{Y}_k \mathbf{E}_S\} \leq 2N_P P_S, \quad (17b)$$

$$\text{tr}\{\mathbf{E}_R^H \mathbf{Y}_k \mathbf{E}_R\} \leq 2N_P P_R, \quad (17c)$$

$$\mathbf{Y}_k \succ \mathbf{0}. \quad (17d)$$

The Lagrangian dual function of (17) is expressed as

$$\begin{aligned} \mathcal{L}(\mathbf{Y}_k, \lambda_k, \gamma_k, \Lambda_k) \\ = \text{tr}\{\mathbf{B}^{-2} \mathbf{Y}_k^{-1}\} + \lambda_k (\text{tr}\{\mathbf{E}_S^H \mathbf{Y}_k \mathbf{E}_S\} - 2N_P P_S) \\ + \gamma_k (\text{tr}\{\mathbf{E}_R^H \mathbf{Y}_k \mathbf{E}_R\} - 2N_P P_R) - \text{tr}\{\Lambda_k \mathbf{Y}_k\} \end{aligned} \quad (18)$$

where  $\lambda_k \geq 0$ ,  $\gamma_k \geq 0$ , and  $\Lambda_k \geq \mathbf{0}$  are the optimum dual variables associated with the constraints in (17b), (17c) and (17d) [25]. The KKT conditions related to  $\mathbf{Y}_k$  are listed as

$$-\mathbf{Y}_k^{-1} \mathbf{B}^{-2} \mathbf{Y}_k^{-1} + \lambda_k \mathbf{E}_S \mathbf{E}_S^H + \gamma_k \mathbf{E}_R \mathbf{E}_R^H - \Lambda_k = \mathbf{0} \quad (19a)$$

$$\lambda_k (\text{tr}\{\mathbf{E}_S^H \mathbf{Y}_k \mathbf{E}_S\} - 2N_P P_S) = 0 \quad (19b)$$

$$\gamma_k (\text{tr}\{\mathbf{E}_R^H \mathbf{Y}_k \mathbf{E}_R\} - 2N_P P_R) = 0 \quad (19c)$$

$$\Lambda_k \mathbf{Y}_k = \mathbf{0}. \quad (19d)$$

To guarantee  $\mathbf{Y}_k \succ \mathbf{0}$ , Eq.(19d) holds only when  $\Lambda_k = \mathbf{0}$ , and both  $\lambda_k$  and  $\gamma_k$  should be positive. Therefore,

$$\mathbf{Y}_k \mathbf{B}^2 \mathbf{Y}_k = \text{diag}\{\lambda_k^{-1}, \lambda_k^{-1}, \gamma_k^{-1}, \gamma_k^{-1}\}. \quad (20)$$

Applying left and right multiplication by  $\mathbf{B}$  to the above equation yields

$$(\mathbf{B} \mathbf{Y}_k \mathbf{B})^2 = \text{diag}\{\lambda_k^{-1}, \lambda_k^{-1}, \rho^2 \gamma_k^{-1}, \rho^2 \gamma_k^{-1}\}. \quad (21)$$

*Lemma 1:* For any diagonal matrix defined as  $\mathbf{S} = \text{diag}\{s_1, s_2, \dots, s_m, \dots, s_M\}$  with  $s_m > 0$ , there exists a unique Hermitian positive definite matrix  $\mathbf{P} = \text{diag}\{\sqrt{s_1}, \sqrt{s_2}, \dots, \sqrt{s_m}, \dots, \sqrt{s_M}\}$  satisfying  $\mathbf{S} = \mathbf{P}^2$ .

*Proof:* See Appendix. ■

Since  $\mathbf{B} \mathbf{Y}_k \mathbf{B}$  is Hermitian positive definite, it has the following unique solution according to Lemma 1,

$$\mathbf{B} \mathbf{Y}_k \mathbf{B} = \text{diag}\{\lambda_k^{-1/2}, \lambda_k^{-1/2}, \rho \gamma_k^{-1/2}, \rho \gamma_k^{-1/2}\}. \quad (22)$$

Subsequently, we obtain

$$\mathbf{Y}_k = \text{diag}\{\lambda_k^{-1/2}, \lambda_k^{-1/2}, \rho^{-1} \gamma_k^{-1/2}, \rho^{-1} \gamma_k^{-1/2}\}. \quad (23)$$

Based on the complementary slackness condition, we obtain  $\text{tr}\{\mathbf{E}_S \mathbf{E}_S^H \mathbf{Y}_k\} - 2N_P P_S = 0$  and  $\text{tr}\{\mathbf{E}_R \mathbf{E}_R^H \mathbf{Y}_k\} - 2N_P P_R = 0$  so that

$$\lambda_k = \frac{1}{(N_P P_S)^2} \quad (24)$$

$$\gamma_k = \frac{1}{(\rho N_P P_R)^2}. \quad (25)$$

As a consequence,

$$\mathbf{Y}_k = \text{diag}\{N_P P_S, N_P P_S, N_P P_R, N_P P_R\}. \quad (26)$$

The above result can be summarized as the following theorem.

*Theorem 1:* For an OFDM-based FD relay network in the presence of IQ imbalances, the optimal pilot matrix  $\mathbf{X}_k^p$  should satisfy the optimality condition  $(\mathbf{X}_k^p)^H \mathbf{X}_k^p = \text{diag}\{N_P P_S, N_P P_S, N_P P_R, N_P P_R\}$  of minimizing the sum of MSE provided that the transmit powers  $P_S$  and  $P_R$  are fixed. ■

*Remark 1:* As  $\mathbf{Y}_k = (\mathbf{X}_k^p)^H \mathbf{X}_k^p$ ,  $\mathbf{X}_k^p$  can be constructed by any four orthogonal columns of an  $N_P \times N_P$  unitary matrix multiplied by  $\sqrt{N_P P_S}$ ,  $\sqrt{N_P P_S}$ ,  $\sqrt{N_P P_R}$  and  $\sqrt{N_P P_R}$ , respectively. Specially, for  $k = 1$  and  $N/2 + 1$ , the first column of  $\mathbf{X}_k^p$  is conjugate to the second one, and the third column is conjugate to the fourth one. Here, we use some special matrices to design their pilot symbols. Considering an  $N_P \times N_P$  normalized discrete Fourier transform matrix, it is easy to find the column  $m$  ( $1 < m \leq N_P$ ) and  $N_P - m + 2$  are conjugate and orthogonal with each other, from which the pilot matrix  $\mathbf{X}_1^p$  and  $\mathbf{X}_{N/2+1}^p$  can be well constructed. Taking  $N_P = 5$  for example, one of the optimal pilot matrix can be formed as

$$\mathbf{X}_k^p = \begin{pmatrix} \sqrt{P_S} & \sqrt{P_S} & \sqrt{P_R} & \sqrt{P_R} \\ \sqrt{P_S} W^1 & \sqrt{P_S} W^4 & \sqrt{P_R} W^2 & \sqrt{P_R} W^3 \\ \sqrt{P_S} W^2 & \sqrt{P_S} W^8 & \sqrt{P_R} W^4 & \sqrt{P_R} W^6 \\ \sqrt{P_S} W^3 & \sqrt{P_S} W^{12} & \sqrt{P_R} W^8 & \sqrt{P_R} W^9 \\ \sqrt{P_S} W^4 & \sqrt{P_S} W^{16} & \sqrt{P_R} W^{10} & \sqrt{P_R} W^{12} \end{pmatrix} \quad (27)$$

with  $W = e^{-j\frac{2\pi}{5}}$ .

However, it doesn't make sense when  $N_P = 4$ . Fortunately, we observe that, for a 4-order standard Hadamard matrix, multiplying its even rows by  $j$ , and each column by  $\sqrt{P_S}$ ,  $\sqrt{P_S}$ ,  $\sqrt{P_R}$  and  $\sqrt{P_R}$ , a feasible form of pilot matrix will be shown as

$$\mathbf{X}_k^p = \begin{pmatrix} \sqrt{P_S} & \sqrt{P_S} & \sqrt{P_R} & \sqrt{P_R} \\ j\sqrt{P_S} & -j\sqrt{P_S} & j\sqrt{P_R} & -j\sqrt{P_R} \\ \sqrt{P_S} & \sqrt{P_S} & -\sqrt{P_R} & -\sqrt{P_R} \\ j\sqrt{P_S} & -j\sqrt{P_S} & -j\sqrt{P_R} & j\sqrt{P_R} \end{pmatrix}. \quad (28)$$

Substituting (26) into (15), we have the minimum Sum-MSE as follows

$$\text{Sum-MSE}_k = \frac{2}{N_P} \left( \frac{1}{P_S} + \frac{1}{\rho^2 P_R} \right) \text{tr}\{\mathbf{C}_w\} \quad (29)$$

**B. OPTIMAL POWER ALLOCATION**

From (29), we find that the minimum Sum-MSE relies heavily on the transmit power of the source and RS. Now, we turn to optimize  $P_S$  and  $P_R$  under the condition  $P_S + P_R \leq P$ . This problem can be formulated as the following geometric program:

$$\begin{aligned} \min_{P_S, P_R} & \frac{2}{N_P} \left( \frac{1}{P_S} + \frac{1}{\rho^2 P_R} \right) \text{tr}(\mathbf{C}_w) \\ \text{s.t.} & P_S + P_R \leq P. \end{aligned} \quad (30)$$

To solve the above convex optimization problem, we construct the associated Lagrangian function as

$$\mathcal{L}(P_S, P_R) = \frac{2}{N_P} \left( \frac{1}{P_S} + \frac{1}{\rho^2 P_R} \right) \text{tr}(\mathbf{C}_w) + \xi(P_S + P_R - P) \quad (31)$$

where  $\xi$  is the Lagrange multiplier. Setting the first-order derivative of the above function with respect to  $P_S$  and  $P_R$  to zero

$$\frac{\partial \mathcal{L}(P_S, P_R)}{\partial P_S} = -\frac{2}{N_P} \frac{1}{P_S^2} \text{tr}(\mathbf{C}_w) + \xi = 0 \quad (32)$$

$$\frac{\partial \mathcal{L}(P_S, P_R)}{\partial P_R} = -\frac{2}{N_P} \frac{1}{\rho^2 P_R^2} \text{tr}(\mathbf{C}_w) + \xi = 0 \quad (33)$$

it is easy to obtain that  $P_S = \rho P_R$  and  $\xi \neq 0$ . This yields  $P_S + P_R - P = 0$  in accordance with the complementary slackness condition, thus the OPA of source and RS becomes

$$P_S = \frac{\rho P}{(1 + \rho)} \quad (34)$$

$$P_R = \frac{P}{(1 + \rho)}. \quad (35)$$

This solution is concluded as the following theorem:

**Theorem 2:** In OFDM-based FD relay networks with IQ imbalances, the optimal power allocation strategy of minimizing the Sum-MSE is given by  $P_S = \frac{\rho P}{(1 + \rho)}$  and  $P_R = \frac{P}{(1 + \rho)}$  subject to the total power constraint of source node and RS  $P_S + P_R \leq P$ . ■

Apparently, when  $\rho > 1$ , more power is allocated to source node. And inversely, when  $\rho < 1$ , RS takes up more power.

In this case, the corresponding minimum Sum-MSE of subcarrier  $k$  and  $\hat{k}$  becomes

$$\text{Sum-MSE}_k^o = \frac{2}{N_P} \left(1 + \frac{1}{\rho}\right)^2 \frac{1}{P} \text{tr}(\mathbf{C}_w). \quad (36)$$

According to (3), the received SNR is defined as

$$\gamma = \frac{(|\mu_{t,S}|^2 + |v_{t,S}|^2)P_S + \rho^2(|\mu_{t,R}|^2 + |v_{t,R}|^2)P_R}{\sigma_v^2} \quad (37)$$

thus the minimum Sum-MSE can be expressed as

$$\begin{aligned} \text{Sum-MSE}_k^o(\rho, \gamma) &= \frac{4(|\mu_{r,R}|^2 + |v_{r,R}|^2)}{\gamma N_P} \\ &\times \left[ \left(1 + \frac{1}{\rho}\right)(|\mu_{t,S}|^2 + |v_{t,S}|^2) + (1 + \rho)(|\mu_{t,R}|^2 + |v_{t,R}|^2) \right]. \end{aligned} \quad (38)$$

The second derivative of the above minimum Sum-MSE with respect to  $\rho$  is

$$\begin{aligned} \frac{\partial^2 \text{Sum-MSE}_k^o(\rho, \gamma)}{\partial \rho^2} &= \frac{8(|\mu_{r,R}|^2 + |v_{r,R}|^2)(|\mu_{t,S}|^2 + |v_{t,S}|^2)}{\rho^3 \gamma N_P} > 0 \end{aligned} \quad (39)$$

for  $\rho > 0$ , which means the minimum Sum-MSE is a convex function of  $\rho$  for  $\rho \in (0, +\infty]$  provided that SNR is fixed. In other words, the function  $\text{Sum-MSE}_k^o(\rho, \gamma)$ , with fixed variable SNR, has a globally minimum value in its domain. Setting the first-order derivative of minimum Sum-MSE with respect to  $\rho$  to zero forms

$$\begin{aligned} \frac{\partial \text{Sum-MSE}_k^o(\rho, \gamma)}{\partial \rho} &= \frac{4(|\mu_{r,R}|^2 + |v_{r,R}|^2)}{\gamma N_P} \\ &\times \left[ -\frac{1}{\rho^2}(|\mu_{t,S}|^2 + |v_{t,S}|^2) + (|\mu_{t,R}|^2 + |v_{t,R}|^2) \right] = 0 \end{aligned} \quad (40)$$

which yields

$$\rho^o = \sqrt{\frac{|\mu_{t,S}|^2 + |v_{t,S}|^2}{|\mu_{t,R}|^2 + |v_{t,R}|^2}}. \quad (41)$$

Finally, we obtain the globally minimum value of Sum-MSE

$$\begin{aligned} \text{Sum-MSE}_k^o(\rho^o, \gamma) &= \frac{4(|\mu_{r,R}|^2 + |v_{r,R}|^2)}{\gamma N_P} \\ &\times \left( \sqrt{|\mu_{t,S}|^2 + |v_{t,S}|^2} + \sqrt{|\mu_{t,R}|^2 + |v_{t,R}|^2} \right)^2 \end{aligned} \quad (42)$$

This result will be further verified in the next section.

**IV. SIMULATION RESULTS**

In what follows, representative numerical simulation results are presented to evaluate the performance of the proposed methods. The system parameters are set as follows: number of OFDM subcarriers  $N = 512$ , length of cyclic prefix  $L = 32$ , signal bandwidth  $BW = 10\text{MHz}$ , number of pilot OFDM symbols  $N_P = 4$ , carrier frequency  $fc = 2\text{GHz}$ , and 16QAM is used for digital modulation.

In Figs. 2-4, the parameters of amplitude and phase imbalances between I and Q branches are chosen as  $\alpha_{t,S} = 5\text{dB}$ ,  $\alpha_{t,R} = \alpha_{r,R} = 1\text{dB}$ , and  $\theta_{t,S} = \theta_{t,R} = \theta_{r,R} = 1^\circ$ . For comparison, the equal power allocation (EPA) of source node and RS is plotted as reference. The Sum-MSE corresponding to EPA is expressed as

$$\begin{aligned} \text{Sum-MSE}_k^e(\rho, \gamma) &= \frac{4(|\mu_{r,R}|^2 + |v_{r,R}|^2)}{\gamma N_P} \\ &\times \left[ \left(1 + \frac{1}{\rho^2}\right)(|\mu_{t,S}|^2 + |v_{t,S}|^2) + (1 + \rho^2)(|\mu_{r,S}|^2 + |v_{r,S}|^2) \right]. \end{aligned} \quad (43)$$

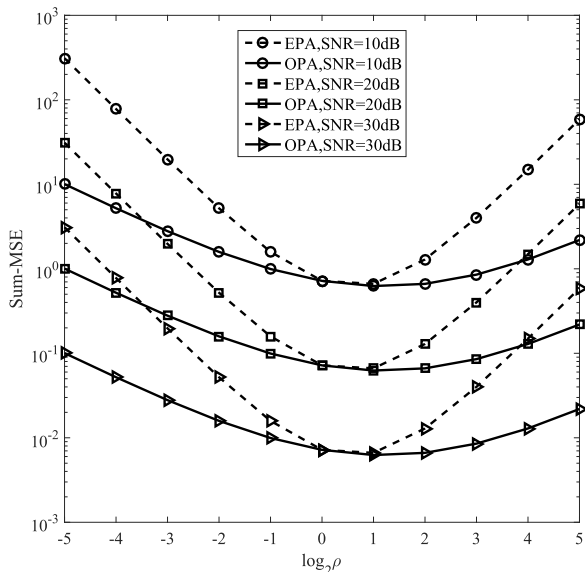


FIGURE 2. Sum-MSE versus  $\rho$  for three typical receive SNRs ( $\alpha_{t,S} = 5dB$ ,  $\alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

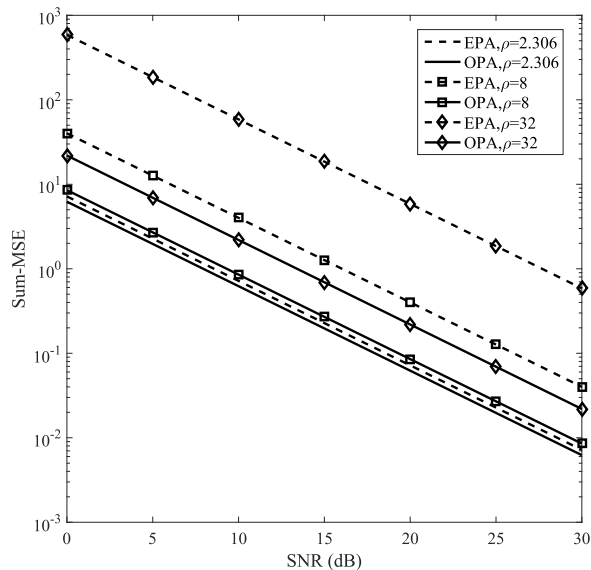


FIGURE 4. Sum-MSE versus receive SNR for for three different values of  $\rho$  ( $\geq \rho^o$ ) ( $\alpha_{t,S} = 5dB$ ,  $\alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

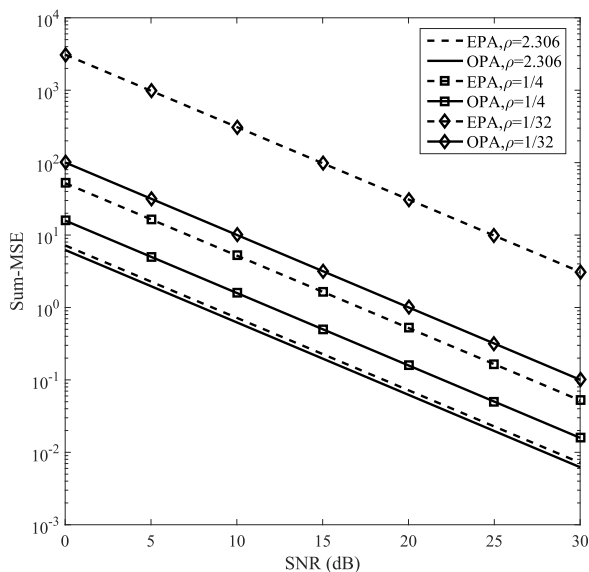


FIGURE 3. Sum-MSE versus receive SNR for three different values of  $\rho$  ( $\leq \rho^o$ ) ( $\alpha_{t,S} = 5dB$ ,  $\alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

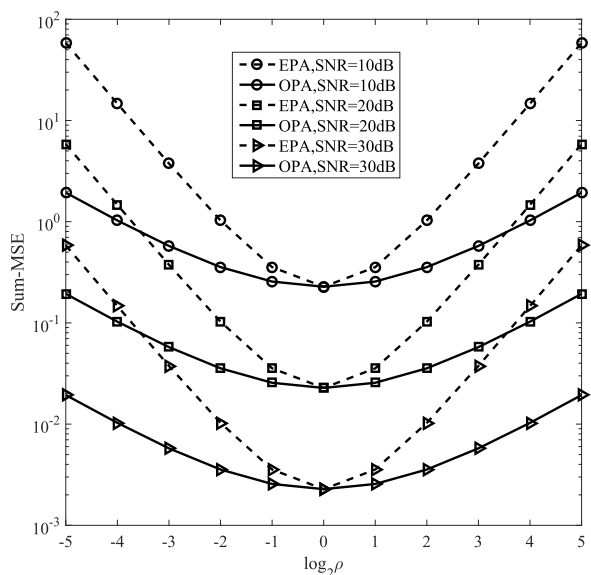


FIGURE 5. Sum-MSE versus  $\rho$  for three typical receive SNRs ( $\alpha_{t,S} = \alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

Fig. 2 demonstrates the curves of Sum-MSE versus  $\rho$  of the proposed pilot pattern and power allocation for three typical receive SNRs. It is seen that the proposed OPA performs better than EPA for all cases ( $\rho > 0$ ). Interestingly, as the value of  $\rho$  is far away from  $\rho^o$ , the Sum-MSE gain achieved by OPA over EPA increases gradually. This implies that the larger performance benefit achieved by OPA is harvested by deviating the value of  $\rho$  from  $\rho^o$ .

Fig. 3 displays the curves of Sum-MSE versus receive SNR of the proposed pilot pattern and power allocation for three different values of  $\rho$  ( $\leq \rho^o$ ). It is seen from this figure that a smaller  $\rho$  leads to a larger Sum-MSE gain achieved by OPA over EPA. For example, OPA makes an approximate

5dB SNR gain over EPA when  $\rho = 1/4$ , and 17dB when  $\rho = 1/32$ . This trend can be explained by the fact that RS needs more power to improve the estimate accuracy of residual SI channel for a small  $\rho$ , i.e., a weak SI channel.

Similar to Fig. 3, Fig. 4 shows the curves of Sum-MSE versus receive SNR of the proposed method for three different values of  $\rho$  ( $\geq \rho^o$ ). The Sum-MSE gain achieved by OPA over EPA becomes larger as  $\rho$  increases. The OPA makes an approximate 7dB SNR gain over EPA when  $\rho = 8$ , while it achieves 16dB SNR gain when  $\rho = 32$ . The main reason is that a large  $\rho$  means the SI channel is stronger than intended channel, hence, more power should be allocated to source node to enhance the estimate precision of intended channel.

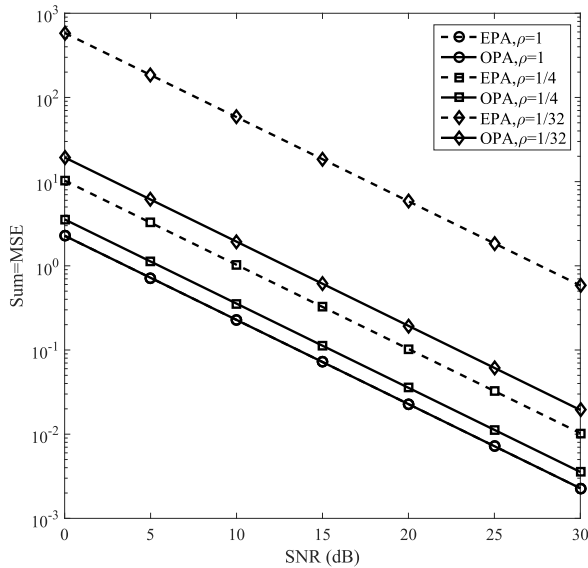


FIGURE 6. Sum-MSE versus receive SNR for three different values of  $\rho (\leq 1)$  ( $\alpha_{t,S} = \alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

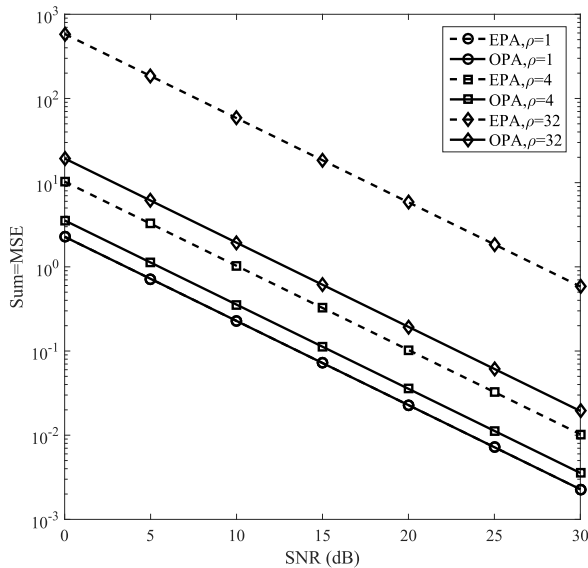


FIGURE 7. Sum-MSE versus receive SNR for three different values of  $\rho (\geq 1)$  ( $\alpha_{t,S} = \alpha_{t,R} = \alpha_{r,R} = 1dB$ ).

In the following, from Fig. 5 to Fig. 7, we set the symmetric parameters of amplitude and phase imbalances between I and Q branches as  $\alpha_{t,S} = \alpha_{t,R} = \alpha_{r,R} = 1dB$ , and  $\theta_{t,S} = \theta_{t,R} = \theta_{r,R} = 1^\circ$ , thus  $\rho^o = 1$ .

Fig. 5 plots the curves of Sum-MSE versus  $\rho$  of the proposed method for three typical receive SNRs. As shown in Fig. 2, the proposed OPA performs better than EPA for all cases. And the Sum-MSE gain achieved by OPA over EPA grows gradually as the value of  $\rho$  deviating from 1. Due to the same parameters of IQ imbalances at source and RS transmitters, the curves of Sum-MSE versus  $\rho$  are symmetric with respect to the line  $\rho = 1$ .

Fig. 6 illustrates the curves of Sum-MSE versus receive SNR of the proposed pilot pattern and power allocation for

three different values of  $\rho (\leq 1)$ . Both EPA and OPA achieve the same minimum Sum-MSE at  $\rho = 1$ . Observing this figure, we find that the Sum-MSE gain achieved by OPA over EPA increases as  $\rho$  decreases. Particularly, the proposed OPA attains an approximate 5dB SNR gain over EPA at  $\rho = 1/4$ , and the SNR gain grows up to 15dB at  $\rho = 1/32$ .

Finally, Fig. 7 indicates the curves of Sum-MSE versus receive SNR of the proposed method for three different values of  $\rho (\geq 1)$ . From Fig. 7, it still follows that the Sum-MSE gain increases as  $\rho$  increases. This figure further verifies the fact that the proposed OPA always performs better than EPA in terms of Sum-MSE performance.

In summary, different from EPA, in our OPA scheme, more power is allocated toward RS to enhance the estimate accuracy of the residual SI channel when  $\rho < 1$ . Otherwise, more power is given to source node to enhance the estimate accuracy of residual SI channel when  $\rho > 1$ .

### V. CONCLUSION

In this paper, we have conducted an investigation of pilot optimization and power allocation for the frequency-domain LS channel estimator in a full-duplex OFDM relay network with IQ imbalances. The analytical expression for optimum pilot product matrix was given by minimizing the Sum-MSE and utilizing the KKT conditions. Following this, the PA problem was formulated as a geometric optimization subject to the total power sum of source and RS. Finally, the optimal PA strategy was proposed and its closed-form solution was derived. Also, the Sum-MSE performance was proved to be a convex function of  $\rho$ , and has a minimum value. Simulation results showed that the Sum-MSE performance of the proposed OPA is better than that of EPA. With the value of  $\rho$  deviating more from the minimum  $\rho^o$ , the Sum-MSE performance gain achieved by OPA over EPA increases gradually. In summary, the proposed PA can radically improve the Sum-MSE performance of the LS channel estimator compared to EPA in the case that  $\rho$  approaches zero from right or tends to positive infinity.

### APPENDIX PROOF OF LEMMA 1

*Proof:* Let  $\mathbf{Q} \neq \mathbf{P}$  be another Hermitian positive definite matrix satisfying  $\mathbf{S} = \mathbf{Q}^2$ . As  $\mathbf{P} - \mathbf{Q} \neq \mathbf{0}$ , there must exist a nonzero real eigenvalue  $a$  and eigenvector  $\xi$  of  $\mathbf{P} - \mathbf{Q}$  such that

$$(\mathbf{P} - \mathbf{Q})\xi = a\xi. \tag{44}$$

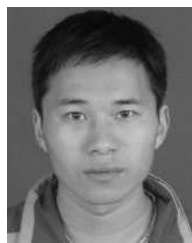
Consequently,

$$\begin{aligned} \xi^H (\mathbf{P}^2 - \mathbf{Q}^2)\xi &= \xi^H \mathbf{P}(\mathbf{P} - \mathbf{Q})\xi + \xi^H (\mathbf{P} - \mathbf{Q})\mathbf{Q}\xi \\ &= a\xi^H (\mathbf{P} + \mathbf{Q})\xi = 0. \end{aligned} \tag{45}$$

Since  $a \neq 0$ , the above equation only holds when  $\xi^H (\mathbf{P} + \mathbf{Q})\xi = 0$ , which contradicts the assumption  $\mathbf{P}$  and  $\mathbf{Q}$  are positive definite. Thus,  $\mathbf{Q} = \mathbf{P}$ , which completes the proof of Lemma 1. ■

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**JIN WANG** received the B.S. degree from the Nanjing University of Science and Technology, Nanjing, China, in 2012, where he is currently pursuing the Ph.D. degree with the School of Electronic and Optical Engineering. His research interests include wireless communications and signal processing.



**HAI YU** received the B.S. degree from the Nanjing University of Science and Technology, Nanjing, China, in 2000, where he is currently pursuing the Ph.D. degree with the School of Electronic and Optical Engineering. His research interests include wireless communications and signal processing.



**YONGPENG WU** (S'08–M'13–SM'17) received the B.S. degree in telecommunication engineering from Wuhan University, Wuhan, China, in 2007, and the Ph.D. degree in communication and signal processing from the National Mobile Communications Research Laboratory, Southeast University, Nanjing, China, in 2013. He is currently a Research Professor (tenure-track) with the Shanghai Key Laboratory of Navigation and Location-Based Services, Shanghai Jiao Tong University, China. Previously, he was a Senior Research Fellow with the Institute for Communications Engineering, Technical University of Munich, Germany, and the Humboldt Research Fellow and the Senior Research Fellow with the Institute for Digital Communications, University of Erlangen-Nurnberg, Germany. During his Ph.D. studies, he conducted co-operative research with the Department of Electrical Engineering, Missouri University of Science and Technology, Rolla, MO, USA. His research interests include massive MIMO/MIMO systems, physical layer security, signal processing for wireless communications, and multivariate statistical theory.



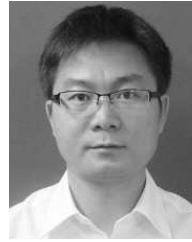


**FENG SHU** (M'16) was born in 1973. He received the B.S. degree from the Fuyang Teaching College, Fuyang, China, in 1994, the M.S. degree from Xidian University, Xi'an, China, in 1997, and the Ph.D. degree from Southeast University, Nanjing, China, in 2002. From 2003 to 2005, he was a Post-Doctoral Researcher with the National Key Mobile Communication Laboratory, Southeast University. In 2005, he joined the School of Electronic and Optical Engineering, Nanjing University of Science and Technology, Nanjing, where he is currently a Professor and a Supervisor of Ph.D. and graduate students. From 2009 to 2010, he was a Visiting Post-Doctoral with The University of Texas at Dallas. He is also with Fujian Agriculture and Forestry University and awarded with Minjiang Scholar Chair Professor in Fujian province. He has authored or co-authored about 200 scientific and conference papers, of which more than 100 are in archival journals, including over 25 papers on IEEE Journals and 50 SCI-indexed papers. He holds five Chinese patents. His research interests include wireless networks, wireless location, and array signal processing. He is currently serving as an Editor for IEEE ACCESS. He has served as session chair or technical program committee member for various international conferences, such as the IEEE WCSP 2016, the IEEE VTC 2016, and so on.



**JIANGZHOU WANG** (F'17) was an IEEE Distinguished Lecturer from 2013 to 2014. He is currently the Head of the School of Engineering and Digital Arts and a Professor of telecommunications with the University of Kent, U.K. He has authored over 200 papers in international journals and conferences in the areas of wireless mobile communications and three books. He is an IET Fellow. He received the Best Paper Award from the 2012 IEEE GLOBECOM. He serves/served as an

Editor for a number of international journals, including an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS from 1998 to 2013 and a Guest Editor of the IEEE JOURNAL ON SELECTED AREAS IN COMMUNICATIONS and the IEEE Communications Magazine. He is currently an Editor of the Science China Information Science. He was the Technical Program Chair of the 2013 IEEE WCNC in Shanghai and the Executive Chair of the 2015 IEEE ICC in London.



**RIQING CHEN** received the B.Eng. degree in communication engineering from Tongji University, China, in 2001, the M.Sc. degree in communications and signal processing from Imperial College London, U.K., in 2004, and the Ph.D. degree in engineering science from the University of Oxford, U.K., in 2010. He is currently a Lecturer with the Faculty of Computer Science and Information Technology, Fujian Agriculture and Forestry University, Fujian, China. His research

interests include network security, spread coding, signal processing, and wireless sensor technologies.



**JUN LI** (M'09–SM'16) received the Ph.D. degree in electronic engineering from Shanghai Jiao Tong University, Shanghai, China, in 2009. In 2009, he was with the Department of Research and Innovation, Alcatel Lucent Shanghai Bell, as a Research Scientist. Since 2015, he has been with the School of Electronic and Optical Engineering, Nanjing University of Science and Technology, Nanjing, China. His research interests include network information theory, channel coding theory,

wireless network coding, and cooperative communications.

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